Problem 6. Let $S$ be the set of all positive rational numbers in lowest terms and with denominator less than 100. Find the element in $S$ that is closest to, but not equal to, $\frac{5}{7}$.

(This must be done without the use of calculator or computer. Correct solutions will have the numerical (fraction) answer and complete supporting work.)