**Problem 4.** Let $ABC$ be a triangle. Prove that there is a point $P$ in the plane of $ABC$ such that $PA = BC$, $PB = CA$, and $PC = AB$ if and only if the triangle is a right triangle.